

# Mathematics 2201 Common Mathematics Assessment

# Sample 2013

Name: Mathematics Teacher:

28 Selected Response13 Constructed Response

FINAL

TIME: 2 HOURS

NOTE

Diagrams are not necessarily drawn to scale.

### FORMULAE

sinA _ sinB _ sinC	$a^2 = b^2 + c^2 - 2bccosA$	$cos A = \frac{b^2 + c^2 - a^2}{cos A - a^2}$	
a - b - c		$cosA = \frac{2bc}{2}$	

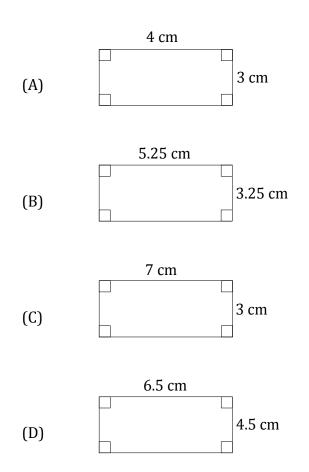
$\sigma = \sqrt{\frac{\sum (x - \bar{x})^2}{n}}$	$z = \frac{x - \mu}{\sigma}$	$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
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28 marks 42 marks

70 Marks

**Selected Response:** Choose the appropriate response on the answer sheet or SCANTRON.

- 1. Lisa draws four parallelograms and measures all sides. She writes the statement *"The opposite sides of a parallelogram are equal"* in her notebook. Which term best describes her statement?
  - (A) conjecture
  - (B) counterexample
  - (C) deductive reasoning
  - (D) inductive reasoning
- 2. What is the missing seventh term in the given sequence?  $\{1, 1, 2, 3, 5, 8, 2, 21\}$ 
  - (A) 11
  - (B) 12
  - (C) 13
  - (D) 14
- 3. Which figure is a counterexample to the statement below? *"The perimeter of a rectangle is never an odd number."*



- 4. If  $\angle 1 = \angle 2$  and  $\angle 1 = \angle 3$ , which property proves that  $\angle 2 = \angle 3$ ?
  - (A) commutative
  - (B) supplementary angles
  - (C) transitive
  - (D) vertically opposite angles

- 5. What is the sum of the interior angles of a convex polygon with 14 sides?
  - 2160° (A) (B) 2340°
  - (C) 2520°
  - 2880° (D)
- An incorrect solution is provided to the question below. In which step did the *first* 6. error occur?

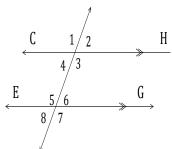
Question:

Given  $CH \parallel EG$  and  $\angle 1 = 120^{\circ}$ , what is the measure of  $\angle 7$ ?

А

b

С



Solution:

Step 1: $\angle 1 = \angle 3$
Step 2: $\angle 3 = \angle 6$
Step 3: $\angle 7 = 180^{\circ} - \angle 6$
<i>Step</i> 4: $\angle 7 = 180^{\circ} - 120^{\circ} = 60^{\circ}$

(A) 1 2 (B) (C) 3 (D) 4

7. What is the length of side *b*? 97° 36 В 15

(A)	8.9
(B)	11.1

- (C) 18.7
- (D) 25.3

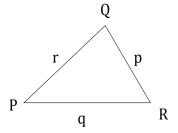
#### Which expression is equal to *sinQ*? 8.

(A) 
$$\frac{q}{r \sin R}$$

(B) 
$$\frac{r}{q sinR}$$

(C) 
$$\frac{q \sin R}{r}$$

(D) 
$$\frac{r \sin R}{q}$$



9.	Simplify completely:	$12\sqrt{40} - 7\sqrt{10}$
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(A)	$5\sqrt{30}$
(B)	$17\sqrt{10}$
(C)	$19\sqrt{30}$
(D)	$41\sqrt{10}$

10. Simplify completely:  $\frac{5\sqrt{15}}{2\sqrt{6}}$ 

(A)	$\frac{5\sqrt{10}}{4}$
(B)	$\frac{15\sqrt{10}}{4}$

(C) 
$$\frac{5\sqrt{90}}{12}$$

(D) 
$$\frac{10\sqrt{90}}{24}$$

11. Simplify completely:  $\sqrt{27x^2}$ 

(A)	$3x\sqrt{3}$
(B)	$3x^2\sqrt{3}$
(C)	$9x\sqrt{3}$
(D)	$9x^2\sqrt{3}$

12. Write  $2y \sqrt[3]{3y}$  as an entire radical.

(A)	$\sqrt[3]{12y^3}$
(B)	$\sqrt[3]{24y^2}$
(C)	$\sqrt[3]{24y^4}$
(D)	$\sqrt[3]{54y^4}$

13. Brad was asked to simplify  $2\sqrt[3]{64x^5}$  but did not complete a correct solution. Which step contains his **first** error?

Solut	tion:	Step 3:	$2 \cdot \sqrt[3]{64} \cdot \sqrt[3]{x^5}$ $2 \cdot 8 \cdot \sqrt[3]{x^3} \cdot \sqrt[3]{x^2}$ $2 \cdot 8 \cdot x \cdot \sqrt[3]{x^2}$ $18x \sqrt[3]{x^2}$
(A) (B) (C) (D)	1 2 3 4		

14. What are the restrictions on the variable for  $\frac{1}{\sqrt{x-1}}$ ?

 (A)
  $x \le 1$  

 (B)
  $x \ge 1$  

 (C)
 x < 1 

 (D)
 x > 1 

15. Which set of data has the lowest standard deviation?

- $(A) \qquad \{0.1, 0.2, 0.3, 0.4, 0.5\}$
- $(B) \qquad \{3.5, 3.6, 3.7, 3.8, 3.9\}$
- (C)  $\{4, 4, 5, 5, 6\}$
- (D) {9,9,9,9,9}
- 16. The ages of participants in a curling bonspiel are normally distributed with a mean of 45 years and a standard deviation of 9 years. What percent of the curlers are between 36 and 54 years of age?
  - (A) 34%
  - (B) 68%
  - (C) 95%
  - (D) 99%
- 17. The heights of all students in a class were measured. It was later discovered that the tape measure used was inaccurate and 5 mm had to be added to each person's height. Which calculation would stay the same based on the new height measures?
  - (A) central tendency
  - (B) mean
  - (C) median
  - (D) standard deviation

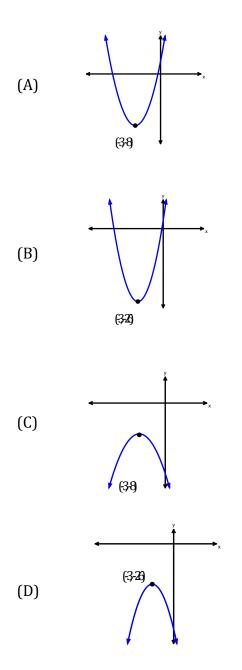
18. What are the domain and range for  $y = 3(x - 1)^2 + 4$ ?

- (A)  $x \in R \text{ and } y \leq 4$ (B)  $x \in R \text{ and } y \geq 4$
- (C)  $x \le 1 \text{ and } y \in R$
- (D)  $x \ge 1 \text{ and } y \in R$
- 19. A quadratic function has an x-intercept at (-7, 0) and an axis of symmetry at x = -1. What is the other x-intercept?
  - $\begin{array}{ll} (A) & (-13,0) \\ (B) & (-4,0) \end{array}$
  - (C) (5,0)
  - (D) (9,0)

20. If (-1, 3) is the vertex of  $y = 2x^2 + bx + 5$ , what is the value of **b**?

- (A) -12(B) -4
- (C) 4
- (D) 12

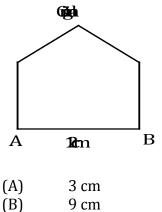
21. The function  $y = x^2 + 6x + 1$  has an axis of symmetry at x = -3. Which graph best models this function?



- 22. Which represents a quadratic function with no x-intercepts?
  - (A)  $y = -(x 1)^2$ (B)  $y = -(x - 1)^2 + 3$ (C)  $y = (x + 1)^2 - 3$ (D)  $y = (x + 1)^2 + 3$
- 23. A gardener has 120 m of fencing to mark off a rectangular vegetable garden. Which function could be used to determine the dimensions that will result in the maximum area?

area.		x
(A) (B)	A = x(x - 60) $A = x(x - 120)$	
(C)	A = x(60 - x)	
(D)	A = x(120 - x)	

- 24. Which function has zeros of -3 and 7?
  - (A) f(x) = (x-3)(x-7)(B) f(x) = (x-3)(x+7)(C) f(x) = (x+3)(x-7)(D) f(x) = (x+3)(x+7)
- 25. What are the roots of the quadratic equation  $x^2 + 6x 16 = 0$ ?
  - (A) x = -8, x = -2
  - (B) x = -8, x = 2
  - (C) x = 8, x = -2(D) x = 8, x = 2
- 26. Which has a unit rate of \$0.16/apple?
  - (A) 20 apples for \$3.00
  - (B) 25 apples for \$4.25
  - (C) 30 apples for \$4.95
  - (D) 35 apples for \$5.60
- 27. The pentagon shown is transformed by a scale factor of  $\frac{1}{4}$ . What is the length of the image of side AB?



- (C) 15cm
- (D) 48 cm
- 28. A partially inflated heart-shaped balloon is 15 cm wide and has a volume of 1600 cm<sup>3</sup>. If air is added until the balloon is 30 cm wide, what is the new volume?

(A)	3200 cm <sup>3</sup>
(B)	6400 cm <sup>3</sup>
(C)	9600 cm <sup>3</sup>
(D)	$12000 \text{ cm}^3$

(D)  $12 800 \text{ cm}^3$ 

### **Constructed Response:**

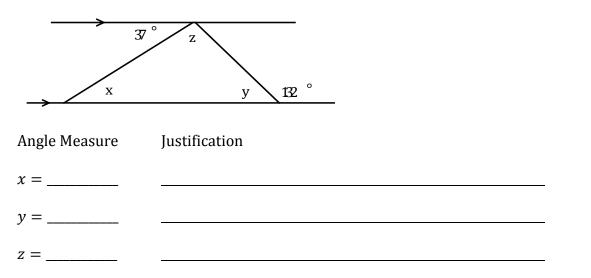
Answers to be written on this paper in the space provided. Show all workings.

29. Use **both** inductive and deductive reasoning to show that the sum of two odd <sup>4 marks</sup> integers is an even number.

Inductive Reasoning

Deductive Reasoning

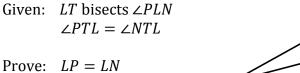
30. Find the measure of each indicated angle. Justify your answer.

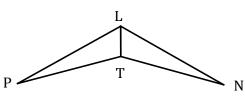


31. Use either a paragraph or two-column format to complete the given proof:

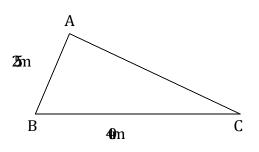
3 marks

3 marks





Page 8 of 13 Eastern School District 32. Peter uses exactly 100 m of string to stake out the triangular plot shown in his back garden. Find the measures of all three angles, to the nearest degree.



33. Simplify: 
$$(3\sqrt{2} - \sqrt{10})^2$$

3 marks

34. State the **restrictions** on *x*, **solve** the equation, and **check** for extraneous roots. 4 marks

 $4 - \sqrt{2x + 1} = 9$ 

Restrictions:\_\_\_\_\_

Solution:\_\_\_\_\_

35. In a pre-election survey in St. John's, 32% of those surveyed were undecided about their choice for mayor. The survey is considered accurate within 8 percentage points, 99 times out of 100. If there are 102 000 eligible voters in St. John's, state the **range** of the number of people who are undecided and the **confidence level**.

2 marks

Range\_\_\_\_\_

Confidence Level\_\_\_\_\_

36. A manufacturer produces tires that have an average thickness of 179 mm, with a standard deviation of 0.9 mm. To be classified as "supreme quality", tires must have a thickness between 177.8 mm and 180.7 mm. What percent, to the nearest whole number, of the total production can be rated as "supreme quality" tires?

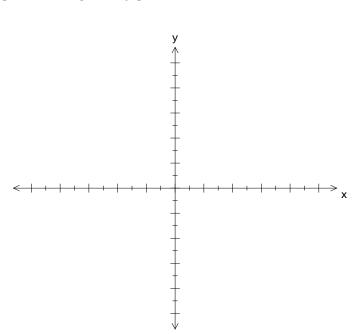
3 marks

37. A model rocket is launched from its launch pad which is 15 m above the ground. It takes 2 seconds for the rocket to reach a maximum height of 35 m. Algebraically determine the quadratic function in the form  $y = a(x - h)^2 + k$ , that models the path followed by the rocket, and use it to determine the height of the rocket at 3.5 s.

Function	

Height\_\_\_\_\_

38. Algebraically determine the **vertex** and **x-intercepts** for the function  $y = -x^2 - 4x + 5$ . Sketch the graph, labelling all key points.



39. Solve the given equation. State the solution(s) in **exact** form.

3 marks

3 marks

 $12x = -5x^2 - 1$ 

40. Use a quadratic function to model and solve the given problem:

A landscaper is designing a 6 m by 8 m rectangular garden that will then be surrounded by a uniform border of crushed stone. She has enough crushed stone to cover 72  $m^2$ . What is the width of the border if she uses all of the crushed stone?



41. Nicole designed a rectangular crest that was 8 cm by 10 cm for her school's jacket. The crest was then enlarged to create a poster that had an area of 980 cm<sup>2</sup>. What are the dimensions of the poster?

3 marks

4 marks

### Mathematics 2201 Common Mathematics Assessment – Sample 2013

Mathematics Teacher:	

1.	А	В	С	D	15.	А	В	С	D
2.	А	В	С	D	16.	А	В	С	D
3.	А	В	С	D	17.	А	В	С	D
4.	А	В	С	D	18.	А	В	С	D
5.	А	В	С	D	19.	А	В	С	D
6.	А	В	С	D	20.	А	В	С	D
7.	А	В	С	D	21.	А	В	С	D
8.	А	В	С	D	22.	А	В	С	D
9.	А	В	С	D	23.	А	В	С	D
10.	А	В	С	D	24.	А	В	С	D
11.	А	В	С	D	25.	А	В	С	D
12.	А	В	С	D	26.	А	В	С	D
13.	А	В	С	D	27.	А	В	С	D
14.	А	В	С	D	28.	А	В	С	D